

**HEIGHT MEASUREMENTS OF THE SPECTRUM AS AN ALTERNATIVE TO
CONVENTIONAL SPECTROPHOTOMETRIC ANALYSIS OF A KMnO_4 -
 $\text{K}_2\text{Cr}_2\text{O}_7$ MIXTURE**

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ABSTRACT

Quantitative spectrophotometric analysis is generally carried out plotting absorbance against concentration, for some concentration range, in accordance with Lambert, Bourger and Bee law. In this work, height measurement of the spectrum was used to analyse KMnO_4 and $\text{K}_2\text{Cr}_2\text{O}_7$ mixtures in two different known concentrations. The experiments were relatively simple to carry out, requiring only standard solutions of KMnO_4 , $\text{K}_2\text{Cr}_2\text{O}_7$, sample mixtures of the two components, a visible light spectrophotometer, recorder, ruler and pencil. Comparison of the two methods showed that the height measurement method is more reliable and versatile as it has no requirement for the calculation of molar absorptivity, shows less relative error than the conventional method.

RESUMO

Análises espectrofotométricas quantitativas geralmente são efetuadas relacionando absorvância e concentração, segundo a lei de Lambert, Bourger e Beer. Neste trabalho, usa-se medidas da altura de espectros para analisar misturas de concentrações conhecidas de KMnO_4 e $\text{K}_2\text{Cr}_2\text{O}_7$. Os experimentos são relativamente simples de serem desenvolvidos, necessitando somente soluções padrões de KMnO_4 , $\text{K}_2\text{Cr}_2\text{O}_7$, misturas dos dois componentes, fonte de luz visível para o espectrofotômetro, registrador, borracha e lápis. Comparando-se os dois métodos, observou-se que o método de medida de altura é mais seguro e versátil, pois não necessita de cálculo de absortividade molar, mostrando menor erro relativo do que o método convencional.

Keywords

Height measurements, spectrophotometric analysis, KMnO_4 - $\text{K}_2\text{Cr}_2\text{O}_7$ mixture, quantification

INTRODUCTION

During the development of a quantitative method for the determination of an unknown concentration of a species using absorption spectrophotometry in the ultraviolet and visible regions, the first step is the choice of the maximum absorption wavelength where the measurements are made. At this wavelength the absorbance of the solution has a linear relation to its concentration within a defined concentration range, following the Lambert, Bourger and Beer law¹. This is the classic method used in quantitative analysis.

To determine two compounds simultaneously by molecular absorption spectrophotometry, these determinations can be made based on absorption measurements at two selected wavelengths, from which a pair of simultaneous equations are obtained, taking into account that the absorbance is an additive property². It is necessary also to measure (or otherwise obtain) the molar absorptivity of each pure compound at the two predetermined wavelengths. When there are more than two compounds in the mixture with superposition of absorption spectrum, more simultaneous equations are required and, consequently software is necessary to resolve them³.

Another quantitative method for mixtures is by using graphs to solve the simultaneous equations. For mixtures of three compounds, the solution to the problem is obtained by a triangular diagram for mixtures of four compounds a tridimensional diagram - a tetrahedron is used⁴.

As an alternative method, when mixtures are involved with overlapping spectra, many wavelengths must be determined so that linear diagrams can be made from which the concentrations can be determined. This method can be applied to mixtures of two or more components⁴.

The measurement of the area of the spectrum and the absorbance band height at different points of the spectrum has also been used successfully⁵.

The purpose of the present work was to show the effectiveness of the spectrum height measurement for the simultaneous quantitative analysis of a mixture of KMnO_4 and $\text{K}_2\text{Cr}_2\text{O}_7$ using the spectrophotometric method.

EXPERIMENTAL PROCEDURE

All the reagents were of analytical grade. Stock solutions of 0.01 mol L^{-1} KMnO_4 and 0.02 mol L^{-1} $\text{K}_2\text{Cr}_2\text{O}_7$ were prepared in previously boiled and cooled deionized water containing 5 mol L^{-1} H_2SO_4 . The concentration of the KMnO_4 solution was determined titrimetrically against $\text{H}_2\text{C}_2\text{O}_4$ 0.01 mol L^{-1} ⁶.

Then, 13 standard solutions of the individual components, were prepared in 50 mL volumetric flasks completing the volumes with deionized water.

Sample mixtures with known concentrations were also prepared as follows: A - 2 mL of 0.01 mol L^{-1} KMnO_4 solution, 5 mL of 0.02 mol L^{-1} $\text{K}_2\text{Cr}_2\text{O}_7$ solution and 5 mL of 5 mol L^{-1} H_2SO_4 solution; B - 1 mL of 0.01 mol L^{-1} KMnO_4 solution, 2 mL of 0.02 mol L^{-1} $\text{K}_2\text{Cr}_2\text{O}_7$ solution and 5 mL of 5 mol L^{-1} H_2SO_4 solution.

The absorption spectra of each standard solution was measured between 400 to 600 nm on a Perkin Elmer 124 spectrophotometer and recorded on a Perkin Elmer 56

recorder. A cell of 1 cm was used while the attenuation was 10 mV and the chart speed was 20 mm.min⁻¹.

Height measurements' were made at 1.1 cm ($\lambda=560$ nm) from the origin for the KMnO₄ spectra (h_1) and at 5.3 cm ($\lambda=449$ nm) of the origin from the K₂Cr₂O₇ spectra (h_3).

Table I lists the data used to make the plot of the KMnO₄ standard solutions while Table II lists the data used to make the plot of the K₂Cr₂O₇ standard solutions.

These heights were plotted against the respective concentrations as shown in Figures 3 and 4.

The spectra of mixture A and B were also recorded from 400 to 600 nm of wavelength. Height measurements were made at the same positions as for the individual solutions.

RESULTS AND DISCUSSION

From height readings' at 1.1 cm from the origin of mixtures' spectra, according Figures 1 and 2, the KMnO₄ concentration can be determined directly from the linear plot of h_1 (height) \times C (concentration), Figure 3. In this situation, there was no interference from the K₂Cr₂O₇ solution, giving a KMnO₄ concentration of 4.0×10^{-4} mol L⁻¹ for mixture A and, for mixture B, a concentration of 2.0×10^{-4} mol L⁻¹.

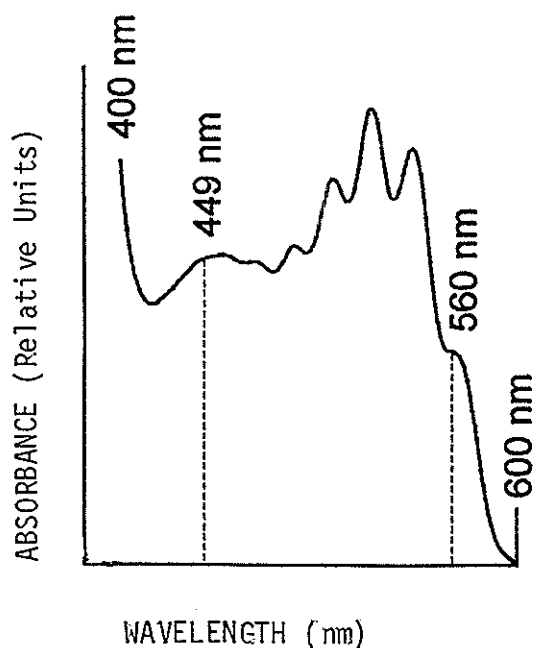


Figure 1. Absorption spectrum of the mixture A.

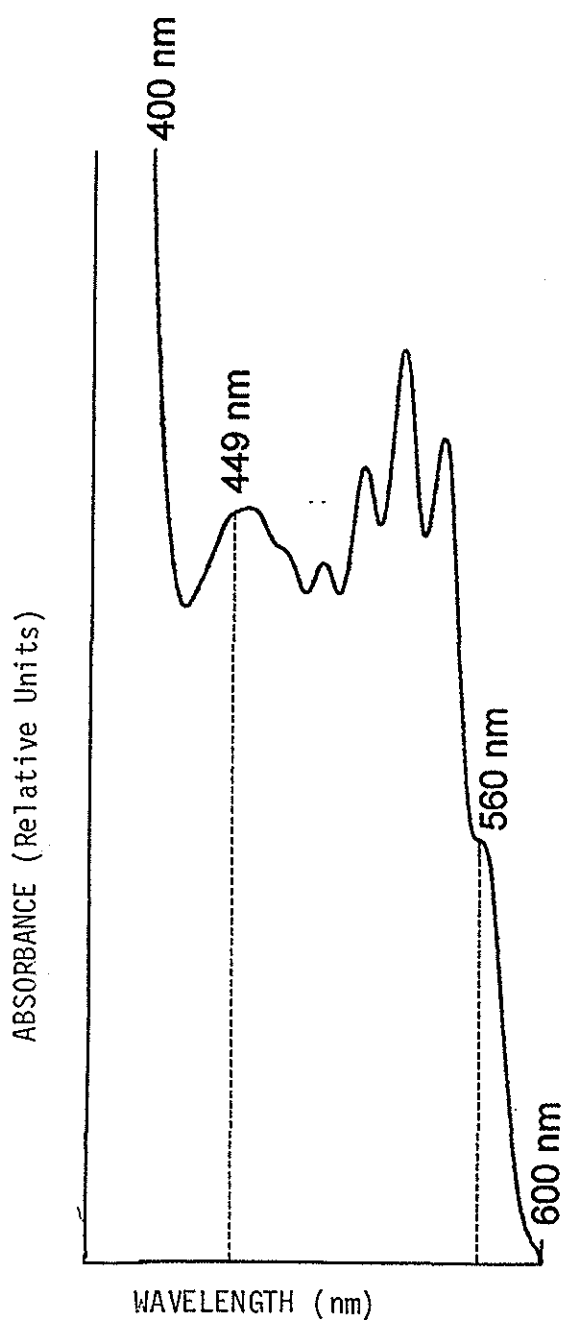


Figure 2. Absorption spectrum of the mixture B.

KMnO_4 standard solutions were prepared on the obtained concentrations from the mixtures and they were used to make the absorption spectra. The heights were measured on the same wavelength that was measured h_t . For mixture A, h_tA it was of 12.5 cm and h_2A it was of 0.8 cm and for mixture B, h_tB it was of 5.1 cm and h_2B of 0.35 cm.

Table I. Spectral height data of KMnO_4 standard solutions measured at 560 nm.

Volume KMnO_4 0.01 mol L^{-1} (mL)	Volume H_2SO_4 5 mol L^{-1} (mL)	Concentration ($\times 10^4 \text{ mol L}^{-1}$)	Concentration (mg L^{-1})	h_1 (height) (cm)
0.4	5	0.8	12.64	1.30
0.7	5	1.4	22.12	2.30
1.0	5	2.0	31.60	3.15
1.3	5	2.6	41.08	3.80
1.6	5	3.2	50.56	5.25
1.9	5	3.8	60.04	6.00
2.2	5	4.4	69.52	7.40
2.5	5	5.0	79.00	8.10
2.8	5	5.6	88.48	9.50
3.1	5	6.2	97.96	10.75
3.4	5	6.8	107.44	12.15
3.7	5	7.4	116.92	13.15
4.0	5	8.0	126.40	14.30

Table II. Spectral height data of $\text{K}_2\text{Cr}_2\text{O}_7$ standard solutions measured at 449 nm.

Volume KMnO_4 0.02 mol L^{-1} (mL)	Volume H_2SO_4 5 mol L^{-1} (mL)	Concentration ($\times 10^3 \text{ mol L}^{-1}$)	Concentration (mg L^{-1})	h_3 (height) (cm)
1.0	5	0.4	117.6	2.8
1.5	5	0.6	176.4	4.0
2.0	5	0.8	235.2	5.5
2.5	5	1.0	294.0	6.3
3.0	5	1.2	352.8	8.0
3.5	5	1.4	411.6	9.0
4.0	5	1.6	470.4	9.0
4.5	5	1.8	592.2	11.5
5.0	5	2.0	588.0	12.5
5.5	5	2.2	646.8	13.8
6.0	5	2.4	705.6	15.5
6.5	5	2.6	764.4	16.2
7.0	5	2.8	823.2	17.6

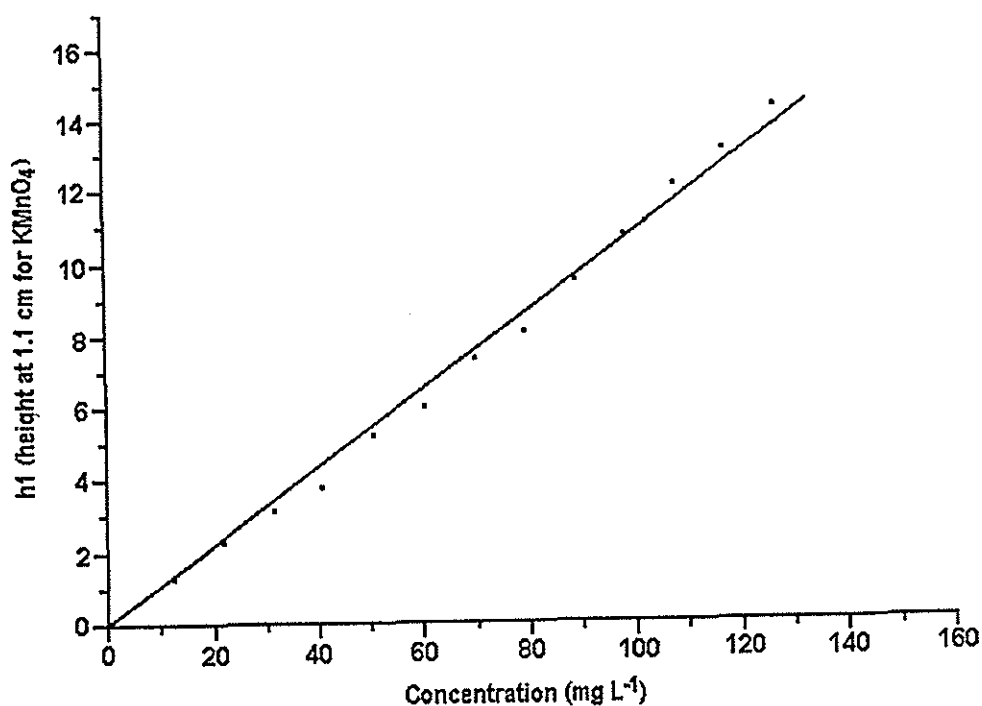


Figure 3. Plot of height (h_1) versus the concentration of KMnO_4 at 1.1 cm. Data from Table I.

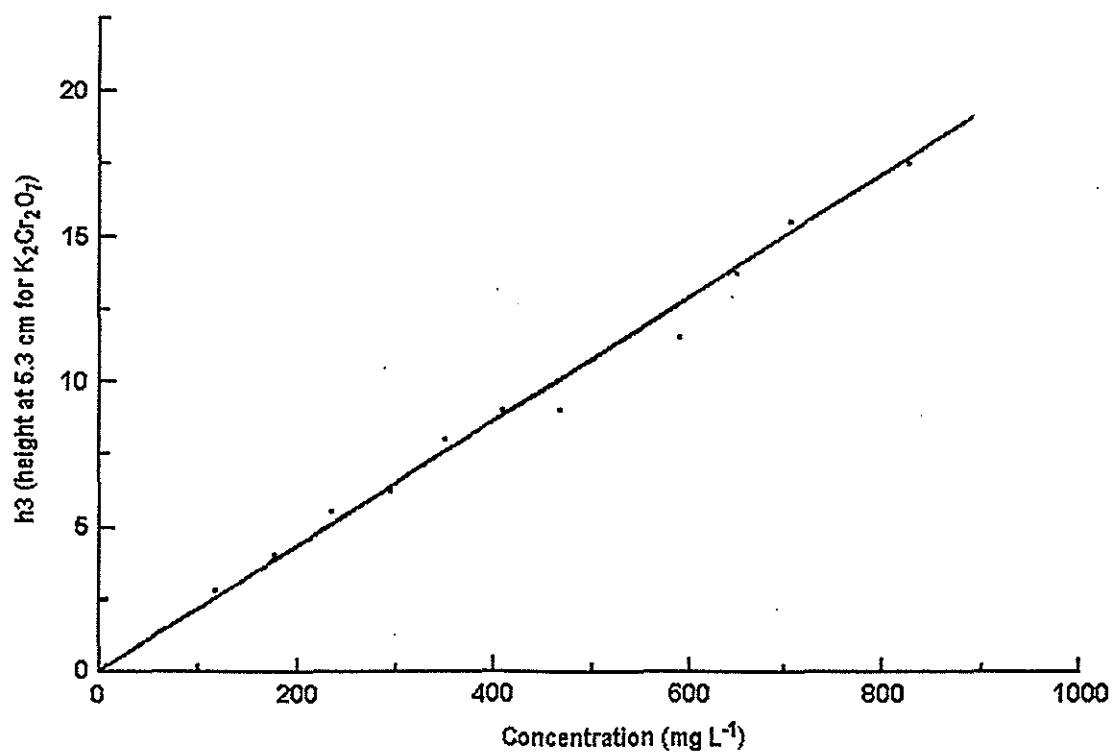


Figure 4. Plot of height (h_3) versus the concentration of $\text{K}_2\text{Cr}_2\text{O}_7$ at 5.3 cm. Data from Table II.

Table III. Results for the two-component mixtures by the conventional and the alternative methods.

Mixtures	Calculated concentration ($\times 10^4 \text{ mol.L}^{-1}$)	Method 1 ($\times 10^4 \text{ mol.L}^{-1}$)	Relative Error (%)	Method 2 ($\times 10^4 \text{ mol.L}^{-1}$)	Relative Error (%)
KMnO ₄	4.0	4.0	0.0	5.0	+ 25.0
A K ₂ Cr ₂ O ₇	20.0	18.0	- 10.0	27.0	+ 35.0
KMnO ₄	2.0	2.0	0.0	2.8	+ 40.0
B K ₂ Cr ₂ O ₇	8.0	7.3	- 8.8	10.0	+ 25.0

Method 1 - Alternative method (Height Measurement)

Method 2 - Conventional method using simultaneous equations

Considering the total height (h_t) measured at 5.3 cm for the mixtures as the sums of the contributions from KMnO₄ and K₂Cr₂O₇:

$$h_t = h_2 + h_3 \quad (1)$$

Then, from: $h_3 = h_t - h_2$, the values of h_3 were calculated (mixture A, $h_3 = 11.7$ cm and mixture B, $h_3 = 4.75$ cm). From Figure 4, the determined K₂Cr₂O₇ concentrations' for mixtures A and B were $1.8 \times 10^{-3} \text{ mol L}^{-1}$ and $7.3 \times 10^{-4} \text{ mol L}^{-1}$, respectively.

Table III gives comparative data for the conventional and this alternative method.

The conventional method uses simultaneous equations, so as many equations as the number of components in the mixture are necessary, requiring values of molar absorptivity as well as absorbances and known concentrations. The relation height versus with this concentration brings the reality nearer than the relation absorbance versus concentration. With this alternative method is not necessary to calculate molar absorptivity and the relative error is smaller compared to the conventional method.

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